

1 次の式を因数分解せよ。

(1)  $(x-2)^2 - 3(x-2) - 18$

$$(x-2)^2 - 3(x-2) - 18 = \{(x-2)+3\}\{(x-2)-6\} \\ = (x+1)(x-8)$$

(2)  $x^4 - 17x^2 + 16$

$$\text{与式} = (x^2)^2 - 17x^2 + 16 = (x^2-1)(x^2-16) \\ = (x+1)(x-1)(x+4)(x-4)$$

(3)  $a(x-2) - x + 2$

$$a(x-2) - x + 2 = a(x-2) - (x-2) = (a-1)(x-2)$$

(4)  $a^2 - 2a^2b + 2b - a$

$$a^2 - 2a^2b + 2b - a = (-2a^2 + 2)b + a^2 - a = -2(a+1)b + a(a-1) \\ = (a-1)\{-2(a+1)b + a\} = (a-1)(-2ab + a - 2b)$$

(5)  $x^2 - 4xy + 4y^2 - 4$

$$x^2 - 4xy + 4y^2 - 4 = (x^2 - 4xy + 4y^2) - 4 = (x-2y)^2 - 2^2 \\ = (x-2y+2)(x-2y-2)$$

(6)  $x^4 - 81$

$$\text{与式} = (x^2)^2 - 9^2 = (x^2+9)(x^2-9) = (x^2+9)(x+3)(x-3)$$

(7)  $(x^2-3x)^2 - 8(x^2-3x) - 20$

$$\text{与式} = \{(x^2-3x)+2\}\{(x^2-3x)-10\} = (x^2-3x+2)(x^2-3x-10) \\ = (x-1)(x-2)(x+2)(x-5)$$

(8)  $2a^2b - 3ab + a - 2b - 2$

$$2a^2b - 3ab + a - 2b - 2 = (2a^2 - 3a - 2)b + a - 2 = (a-2)(2a+1)b + (a-2) \\ = (a-2)\{(2a+1)b + 1\} = (a-2)(2ab + b + 1)$$

(9)  $x^2 + 5xy + 6y^2 - 2x - 7y - 3$

$$x^2 + 5xy + 6y^2 - 2x - 7y - 3 = x^2 + (5y-2)x + (6y^2 - 7y - 3) \\ = x^2 + (5y-2)x + (2y-3)(3y+1) \\ = \{x + (2y-3)\}\{x + (3y+1)\} \\ = (x+2y-3)(x+3y+1)$$

$$\begin{array}{r} 1 \quad \times \quad 2y-3 \quad \longrightarrow \quad 2y-3 \\ 1 \quad \times \quad 3y+1 \quad \longrightarrow \quad 3y+1 \\ \hline 1 \quad (2y-3)(3y+1) \quad 5y-2 \end{array}$$

2 次の値を求めよ。

(1)  $|\sqrt{3} - 2|$

$$\sqrt{3} = 1.732\cdots \text{であるから } \sqrt{3} - 2 < 0 \\ \text{よって } |\sqrt{3} - 2| = -(\sqrt{3} - 2) = 2 - \sqrt{3}$$

(2)  $|-3| - |9|$

$$|-3| - |9| = 3 - 9 = -6$$

(3)  $|7+4| - |-6+2| + |3-5|$

$$|7+4| - |-6+2| + |3-5| = |11| - |-4| + |-2| = 11 - 4 + 2 = 9$$

3  $x = \frac{2}{\sqrt{6}-2}$ ,  $y = \frac{2}{\sqrt{6}+2}$  のとき、次の式の値を求めよ。

(1)  $x + y$

$$x + y = \frac{2}{\sqrt{6}-2} + \frac{2}{\sqrt{6}+2} = \frac{2(\sqrt{6}+2) + 2(\sqrt{6}-2)}{(\sqrt{6}-2)(\sqrt{6}+2)} = \frac{4\sqrt{6}}{6-4} = 2\sqrt{6}$$

(2)  $xy$

$$xy = \frac{2}{\sqrt{6}-2} \times \frac{2}{\sqrt{6}+2} = \frac{4}{(\sqrt{6}-2)(\sqrt{6}+2)} = \frac{4}{6-4} = 2$$

(3)  $x^2 + y^2$

$$x^2 + y^2 = (x+y)^2 - 2xy = (2\sqrt{6})^2 - 2 \cdot 2 = 20$$

(4)  $x^3y + xy^3$

$$x^3y + xy^3 = xy(x^2 + y^2) = 2 \cdot 20 = 40$$

4 次の循環小数  $0.\dot{4}5\dot{6}$  を分数で表せ。

$$\begin{array}{r} x = 0.\dot{4}5\dot{6} \text{ とおく。} \\ x = 0.456456\cdots \\ 1000x = 456.456456\cdots \\ \hline -) \quad x = 0.456456\cdots \\ \hline 999x = 456 \end{array}$$

1000x と x の差を考えると、右の計算から

$$999x = 456 \quad \text{よって} \quad x = \frac{456}{999} = \frac{152}{333}$$

5] 次の式を計算せよ。

(1)  $4\sqrt{50} - 2\sqrt{32} - \sqrt{72}$

$$\begin{aligned} 4\sqrt{50} - 2\sqrt{32} - \sqrt{72} &= 4\sqrt{5^2 \cdot 2} - 2\sqrt{4^2 \cdot 2} - \sqrt{6^2 \cdot 2} \\ &= 20\sqrt{2} - 8\sqrt{2} - 6\sqrt{2} \\ &= (20 - 8 - 6)\sqrt{2} = 6\sqrt{2} \end{aligned}$$

(2)  $(\sqrt{7} + \sqrt{2})(\sqrt{7} - \sqrt{2})$

$$(\sqrt{7} + \sqrt{2})(\sqrt{7} - \sqrt{2}) = (\sqrt{7})^2 - (\sqrt{2})^2 = 7 - 2 = 5$$

(3)  $(\sqrt{5} - \sqrt{10})^2$

$$\begin{aligned} (\sqrt{5} - \sqrt{10})^2 &= (\sqrt{5})^2 - 2\sqrt{5}\sqrt{10} + (\sqrt{10})^2 \\ &= 5 - 2\sqrt{50} + 10 = 5 + 10 - 2\sqrt{5^2 \cdot 2} = 15 - 10\sqrt{2} \end{aligned}$$

別解  $(\sqrt{5} - \sqrt{10})^2 = \{\sqrt{5}(1 - \sqrt{2})\}^2 = (\sqrt{5})^2(1 - \sqrt{2})^2$   
 $= 5(1 - 2\sqrt{2} + 2) = 5(3 - 2\sqrt{2})$   
 $= 15 - 10\sqrt{2}$

6] 次の式を計算せよ。

(1)  $\frac{1}{\sqrt{5}} - \frac{1}{\sqrt{20}} - \frac{1}{\sqrt{125}}$

$$\begin{aligned} \frac{1}{\sqrt{5}} - \frac{1}{\sqrt{20}} - \frac{1}{\sqrt{125}} &= \frac{1}{\sqrt{5}} - \frac{1}{2\sqrt{5}} - \frac{1}{5\sqrt{5}} \\ &= \frac{\sqrt{5}}{\sqrt{5} \cdot \sqrt{5}} - \frac{\sqrt{5}}{2\sqrt{5} \cdot \sqrt{5}} - \frac{\sqrt{5}}{5\sqrt{5} \cdot \sqrt{5}} \\ &= \frac{\sqrt{5}}{5} - \frac{\sqrt{5}}{10} - \frac{\sqrt{5}}{25} = \frac{10\sqrt{5} - 5\sqrt{5} - 2\sqrt{5}}{50} \\ &= \frac{3\sqrt{5}}{50} \end{aligned}$$

(2)  $\frac{\sqrt{5}}{\sqrt{3} + \sqrt{2}} + \frac{5\sqrt{5}}{\sqrt{8} + \sqrt{3}}$

$$\begin{aligned} \frac{\sqrt{5}}{\sqrt{3} + \sqrt{2}} + \frac{5\sqrt{5}}{\sqrt{8} + \sqrt{3}} &= \frac{\sqrt{5}(\sqrt{3} - \sqrt{2})}{(\sqrt{3} + \sqrt{2})(\sqrt{3} - \sqrt{2})} + \frac{5\sqrt{5}(\sqrt{8} - \sqrt{3})}{(\sqrt{8} + \sqrt{3})(\sqrt{8} - \sqrt{3})} \\ &= \frac{\sqrt{5}(\sqrt{3} - \sqrt{2})}{3 - 2} + \frac{5\sqrt{5}(\sqrt{8} - \sqrt{3})}{8 - 3} \\ &= \sqrt{5}(\sqrt{3} - \sqrt{2}) + \sqrt{5}(\sqrt{8} - \sqrt{3}) \\ &= \sqrt{15} - \sqrt{10} + 2\sqrt{10} - \sqrt{15} \\ &= \sqrt{10} \end{aligned}$$